Enhanced Kerr electro-optic nonlinearity and its application in controlling second-harmonic generation

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We proposed a new scheme of controlling second-harmonic generation by enhanced Kerr electro-optic nonlinearity. We designed a structure that can implement the cascaded Pockels effect and second-harmonic generation simultaneously. The energy coupling between the fundamental lights of different polarizations led to a large nonlinear phase shift and, thus, an effective electro-optic nonlinear refractive index. The effective nonlinearity can be either positive or negative, causing the second-harmonic spectra to move toward the coupling center, which, in turn, offered us a way to measure the effective electro-optic nonlinear refractive index. The corresponding enhanced Kerr electro-optic nonlinearity is more than three orders of magnitude higher than the intrinsic value. These results open a door to manipulate the nonlinear phase by applying an external electric field instead of light intensity in noncentrosymmetric crystals. © 2015 Chinese Laser Press

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1. INTRODUCTION

Third-order nonlinearities, though with weak third-order coefficients [1,2], exist in a medium with any symmetry [3–5]. One common way to enhance the intrinsic weak third-order nonlinearity is via cascading second-order nonlinear effects [6] because of its much higher value than the direct higher-order nonlinearity [7–9]. The Kerr electro-optic (EO) effect is connected to the appearance of the nonlinear third-order susceptibility [1]. It takes advantage of the modulation of the electric field and intrinsic nature of fast response time. Besides applications in electro-optic switching [10], electro-optical detection [11], high-speed optical shutters [12], it is also used to measure the optical third-order susceptibility of material [13]. However, the Kerr EO effect is relatively weak in noncentrosymmetric crystals for the existence of a linear EO effect [1]. Therefore, it is highly demanded to enhance Kerr EO nonlinearity and broaden its applications in noncentrosymmetric crystals.

In our previous work, we proposed a new phenomenon named cascaded polarization coupling generated in MgO doped periodically poled lithium niobate (PPLN) near its phase-matching condition [14]. However, there remains some deficiencies: (1) the experiment cannot measure the enhancement of Kerr EO nonlinearity or the effective Kerr EO coefficient; (2) the equation of phase shift did not apply for small phase-mismatching conditions; (3) it just studied the relationship between the phase shift and external electric field, and the fixed input wavelength made it difficult in practical flexibility and adjustability.

Therefore, in this paper, we mainly propose one of its potential applications in modulating second-order nonlinearity by achieving the cascaded effects and second-harmonic generation (SHG) simultaneously in a single PPLN. We also deduced the exact equation of phase shift and studied its relationship with phase-mismatching. The nonlinearity can be either positive or negative, depending on the sign of phase-mismatching. The induced nonlinear refractive index effectively affected the wave-vector mismatching of SHG and controlled the process. In turn, the shift of SHG spectra offered a way to measure the enhancement, which is more than three orders of magnitude higher than its intrinsic value. In addition, we used the tunable laser for our light source, by which we can choose different domain periods or wave-lengths as needed to perform the experiment. Comparing with the ordinary way to control SHG by changing the temperature, our scheme also takes advantage of fast response time and large tunability.

2. MATERIALS AND METHODS

When an external electric field is applied along the y axis of a LiNbO3 crystal [1], the principal axes of the new index ellipsoid rotates with an angle of \( \theta = (\gamma_{31} E_y - s_{41} E_y^2)/(1/(n^2_o) - 1/(n^2_w)^2) \), with respect to the unperturbed principal axes. Taking linear and Kerr EO effects into account, we deduce the refractive index of the new optical axis due to the equation of the index ellipsoid:
\[ n^2_{2} = n^0_{2} - \frac{1}{2} s_{13} (n^0_{e})^3 E^2_y + \frac{1}{2} (\gamma_{31} E_y - s_{41} E^2_y) (n^0_{e})^3 \tan \theta. \]  

where \( n^0_{2} \) and \( n^0_{e} \) represent the indices of the fundamental extraordinary and ordinary waves, \( \gamma_{31} \) and \( s_{13} \), and \( s_{41} \) are the linear and quadratic electro-optic coefficients, and \( E_y \) is the \( y \)-axis external electric field, respectively. As for periodically poled LiNbO\(_3\) crystal [Figs. 1(b) and 1(c)], the \( c \) axis of the LiNbO\(_3\) is inverted periodically, which leads to the periodic alteration of the sign of nonlinear optical susceptibility and electro-optic coefficients. Therefore, when the electric field is applied along the \( y \) axis of PPLN, the optical axis of each domain rotates periodically, as shown in Fig. 1(a) [1,15]. Then, the energy of the incident \( e \)-polarized wave will flow to the generated \( o \)-polarized wave, and then it will flow back. If this occurs near its phase-matching condition, the returning \( o \)-polarized wave will have a different phase from the original \( e \)-polarized wave, which does not deplete completely as dedicated in Figs. 1(b) and 1(c).

Amplitude of the \( e \)-polarized wave is solved by the coupled-mode equations [1], which is \( A(z) = e^{i(\Delta \beta/2)z}[\cos(\Delta \beta z) + i\Delta \beta \sin(\Delta \beta z)/(2\Delta \beta)] \). \( \Delta \beta = (n^0_{e} - n^0_{o}) 2\pi/\lambda - \pi /\Lambda \) is the wave-vector mismatching for cascaded linear EO effects, \( s = [\kappa \Omega^2 + (\Delta \beta/2)^2]^1/2, \kappa [16] \) is the coupled coefficient, \( \Lambda \) is the domain period of PPLN, and \( \lambda \) is the fundamental wavelength, respectively. Then, we obtain the nonlinear phase change impressed onto the fundamental \( e \)-polarized wave at the exit surface \( z = L \), which is

\[ \Delta \Phi^e_{NL} = \frac{\Delta \beta L}{2} - \arctan \left[ \frac{\Delta \beta}{2s} \tan(sL) \right]. \]

where \( L \) is the length of the crystal. We can also achieve an EO effective nonlinear refractive index \( \Delta n^e_{2} \) deduced by \( \Delta \Phi^e_{NL} \), since \( \Delta \Phi^e_{NL} = (2\pi L/\lambda) \Delta n^e_{2} \) [17]. We plot the calculated transmission spectrum [18] and the effective EO nonlinear refractive index as a function of \( \Delta \beta / L \) in Fig. 2. The effective nonlinearity can be either positive or negative, depending on the sign of \( \Delta \beta \). We can see that \( \Delta \Phi^e_{NL} > 0, \Delta n^e_{2} > 0 \) for \( \Delta \beta < 0 \) and \( \Delta \Phi^e_{NL} < 0, \Delta n^e_{2} < 0 \) for \( \Delta \beta > 0 \). It is similar to the phase shift caused by cascaded \( \chi^{(2)} \chi^{(2)} \) process [8,19]. \( \Delta \beta = 0 \) corresponds to the central fundamental wavelength \( \lambda_c \) of the transmission spectrum. \( \Delta \beta < 0 \) refers to the region that the fundamental wavelength \( \lambda < \lambda_c \), and \( \Delta \beta > 0 \) refers to the region that \( \lambda > \lambda_c \).

In the limit of weak cascaded effects and negligible depletion of the fundamental wave, the nonlinear phase shift is approximately proportional to the square of the electric field \( E_y \). And the effective EO nonlinear refractive index is deduced in [14] as

\[ \Delta n^e_{2} \approx \frac{2(n^0_{e} n^0_{o})^3 E^2_y}{\pi \lambda \Delta \beta}. \]

Here, \( |\Delta \beta| \gg |\kappa| \) should be satisfied under large phase mismatching or a low external electric field. In this case, \( \Delta n^e_{2} \) is approximately proportional to the square of the external electric field and independent of the incident optical intensity.

![Fig. 1. (a) Rotation of the optical axes under applied \( y \)-direction external electric field. (b) Schematic of achieving cascaded linear EO effects and SHG simultaneously in a single PPLN. The periodically inverted optical axes of PPLN lead to the periodic alteration of the sign of electro-optic coefficients \( \pm \gamma_{ij} \). (c) Illustration of cascaded linear EO effects. (d) Changes of refractive indices caused by linear, Kerr, and cascaded linear EO effects, respectively. (e) Part of etched poling surface of the sample, with domain inversion period of 20.3 \mu m.](image)

![Fig. 2. Calculated transmission spectrum and the effective EO nonlinear refractive index as a function of \( \Delta \beta / L \). \( \Delta \beta = 0 \) corresponds to the central wavelength \( \lambda_c \) of the transmission spectrum.](image)

![Fig. 3. (a) Measured transmission and SHG spectra fully overlapped at \( T = 26.3^\circ C \). SHG spectra with varied external electric fields at (b) 26.3°C; (c) 24.1°C; (d) 27.6°C. The intensity of SHG was modulated by the enhanced Kerr EO nonlinearity.](image)
The calculated value is shown in Fig. 1(d). Points A, B, and C mark the index changes at 0.1 V/µm. Otherwise, the approximation breaks down, and Eq. (3) must be solved exactly.

Thus, the index variations induced by different EO effects should be expressed by \( \Delta n = \Delta n_1 + \Delta n_2 + \Delta n_{\text{eff}} \), as shown in Fig. 1(d). \( \Delta n_1 \) and \( \Delta n_2 \) are the changes of refractive indices by the linear and intrinsic Kerr EO effects, whose relationships with electric fields are plotted in Fig. 4(a). The EO coefficients of LiNbO\(_3\) are \( r_{31} = 32.6 \times 10^{-12} \text{ m/V} \) [1] and \( s_{31} = 2.3 \times 10^{-20} \text{ m}^2/\text{V}^2 \) [20], respectively. Supposing the external electric field is 0.1 V/µm (\( \lambda = 1581.9 \text{ nm}, \Delta \beta > 0 \)), the magnitude of the rotation angle \( \theta \) is 10\(^{-4}\). Therefore, we can obtain \( \Delta n_1 = 1.6 \times 10^{-5}, \Delta n_2 = 1.1 \times 10^{-10}, \) and \( \Delta n_{\text{eff}} = -1.1 \times 10^{-6} \), which are marked as points A, B, and C in Fig. 4, respectively. \( \Delta n_1 \) and \( \Delta n_2 \) can be ignored if compared with \( \Delta n_{\text{eff}} \), which makes all the index changes \( \Delta n \approx \Delta n_{\text{eff}} \). We can obtain an effective Kerr EO coefficient, \( s_{\text{eff}}^{\text{Kerr}} = -2\Delta n_{\text{eff}}^2/[(n_0^2)^3E_y^2] \) from Eqs. (1) and (2). The calculated value is \( s_{\text{eff}}^{\text{Kerr}} \approx 2.2 \times 10^{-17} \text{ m}^2/\text{V}^2 \). It is more than three orders of magnitude higher than the intrinsic value [20].

For quasi-phase-matching [21,22] SHG [23,24], the wave-vector mismatching is given by \( \Delta k = (n_0^2 - n_c^2)4\pi/\lambda - 2\pi/N \) with the domain period of \( \Lambda^\prime \). \( n_c^2 \) is the index of second-harmonic extraordinary wave. Refractive indices are calculated by Sellmeier equations [25]. Supposing \( \Lambda = \Lambda^\prime \), the two processes can be realized in a single PPLN with a proper incident wavelength and temperature simultaneously. The induced EO nonlinear refractive index affects the original wave-vector mismatching of SHG effectively, which makes it turn into

\[
\Delta k' = \left[n_c^0 - n_0^2 + \Delta n_{\text{eff}}^0\right]4\pi/\lambda - 2\pi/N. \quad (4)
\]

Figure 1(c) shows one part of the etched poling surface of the \( z \)-cut 5% MgO-doped periodically poled LiNbO\(_3\) crystal, with a domain inversion period of 20.3 µm and a dimension of 40 × 10 × 0.5 (nm). The external electric field is applied along the \( y \) axis of PPLN, and light propagates along the \( z \) axis. The light from the tunable continuous laser (1517–1628 nm) was amplified to 100 mW (corresponding to 1.6 × 10\(^5\) W/cm\(^2\)) by an erbium-doped fiber amplifier. The sample was placed between two parallel polarization beam splitters to measure the transmittance of the fundamental wave [18]. A high-voltage source with the maximum of 10 kV was used to generate the external electric field along the \( y \) axis of the PPLN. One power meter working on c-band measured the transmission of the output fundamental wave, while another power meter working on visible light measured the intensity of the second-harmonic wave, respectively.

**3. RESULTS AND DISCUSSION**

We observed that the two processes, namely, the cascaded linear EO effects and SHG, occurred simultaneously at the wavelength of 1582.1 nm and the same temperature of 26.3°C. The overlapped spectra are plotted in Fig. 3(a). When the experimental temperature changed, the two spectra separated from each other at an opposite direction. We measured the intensity of SHG for different external electric fields at a fixed experimental temperature. Figures 3(b)–3(d) show the results at different temperatures. The shift of the SHG spectra is due to the variable effective EO nonlinear refractive index induced by different electric fields.

As seen in Figs. 3(a) and 3(b), at 26.3°C, the absolute value \( |\Delta k'| \) became larger at both sides of SHG spectrum along with the increase of the applied electric field because the spectra are fully overlapped. It led to a dramatic decrease of the SHG efficiency. At 24.1°C, as shown in Fig. 3(c), SHG spectrum is located at the left region of transmission gap (\( \lambda < \lambda_c, \Delta \beta > 0 \)), in which \( \Delta n_{\text{eff}}^0 < 0 \). \( |\Delta k'| \) became larger at the left side and smaller at the other side of the SHG spectrum. As a result, the whole SHG spectrum moved right. Oppositely, at 27.6°C in Fig. 3(d), the SHG spectrum located at the right region of transmission gap (\( \lambda > \lambda_c, \Delta \beta < 0 \)). The positive \( \Delta n_{\text{eff}}^0 \) led to the SHG spectrum shifting left.

Figure 3 suggests how the enhanced Kerr EO nonlinearity controls the process of SHG. On the basis of which, we can measure the magnitude of \( \Delta n_{\text{eff}}^0 \) according to the shift of the SHG central wavelength. The experimental results calculated from Figs. 3(c) and 3(d) are plotted in Fig. 4(b), where \( \Delta n_{\text{eff}}^0 < 0 \) in Fig. 3(c) and \( \Delta n_{\text{eff}}^0 > 0 \) in Fig. 3(d), respectively. They satisfy the condition of large phase-mismatching, and the variations of the effective nonlinear indices are proportional to the square of the external electric field. It is in good agreement with the simulation results deduced by Eq. (3). At \( E_y = 0.1 \text{ V/µm} \) (1581.9 nm, \( \Delta \beta > 0 \)), the experimental values are \( \Delta n_{\text{eff}}^0 = -6.4 \times 10^{-7} \), and we obtain \( s_{\text{eff}}^{\text{Kerr}} \approx 1.3 \times 10^{-17} \text{ m}^2/\text{V}^2 \), which are identical to the theoretical values.

In general, there are three other possible effects that may contribute to the shift of the SHG spectra, including the intensity of the fundamental light, the index change caused by intrinsic EO effects, and the cascaded nonlinearity between the second-harmonic and fundamental wave. However, in our scheme, all of them are not possible to come into play.

![Fig. 5. Measured normalized transmission (a) and SHG intensity (b) at two selected wavelengths [1581.8 and 1582.3 nm in Fig. 3(c)] as a function of the external electric fields. At \( E_y = 0.32 \text{ V/µm}, \) the two wavelengths have the same transmittances but quite different SHG intensities.](image-url)
First, since the intensity of SHG is proportional to the square of the intensity of the fundamental wave [2], we observed the normalized transmission and SHG intensity as a function of the applied electric field. As demonstrated in Fig. 5, we selected two wavelengths of 1581.8 and 1582.3 nm from each sideband of the SHG spectrum in Fig. 3(c). At $E_y = 0.32$ V/µm, the same normalized transmittances were measured for these two different wavelengths. However, for their normalized SHG intensities, the one is high to 0.81 at A and the other is low to 0.29 at B. It means that, although the intensity of incident light varies with the external electric field, it hardly affects the efficiency of SHG. Second, when the temperature was high enough that the transmission spectrum is barely overlapped with SHG, we observed that the SHG spectrum remained unchanged when varying the external electric fields. It agrees well with our discussion that the index variation caused by intrinsic EO effects are small, so it can be neglected. Last, the cascaded second-order nonlinear process is invalid in this case because the incident optical intensity is pretty low ($1.6 \times 10^8$ W/cm²).

We also observed the same phenomena at domain periods of 20.1 and 19.9 µm, which makes it significant to explore the further intrinsic bond between the two physical processes. The wave-vector mismatchings are determined by the dispersion relations [25], as a function of the wavelength, domain inversion period, and temperature. Supposing $\Delta \beta$ and $\Delta k$ equal to 0 simultaneously, the relationship between the domain period and wavelength is plotted in Fig. 6. Points a, b, and c correspond to the three inversion domain periods we performed in our experiment. The inaccuracy of Sellmeier equations causes the theoretical wavelength (1583.1 nm) for 20.3 µm, which is a little shift from the experimental condition (1582.1 nm). By careful calculation, we confirm that these two processes can be satisfied simultaneously at a designed domain inversion period if employing a proper wavelength and temperature. The corresponding relationship is inserted in Fig. 6. Therefore, if given one of the three parameters in Fig. 5, we can find the other two, which is significant in practical flexibility and adjustability.

4. CONCLUSIONS
In conclusion, we demonstrated a new scheme of manipulating the second-order nonlinear effect by enhanced Kerr EO nonlinearity. The enhanced Kerr EO nonlinearity is more than three orders of magnitude higher than the intrinsic value. Moreover, besides SHG, other second-order parametric processes such as sum and difference frequency generation can also be manipulated by this enhanced Kerr EO nonlinearity. The principal basis of this Kerr EO nonlinearity is quite different from that induced by cascaded second-order nonlinear processes, for its independence of the light intensity. Therefore, it can find potential applications in electrically controlled third-order nonlinearities, such as group velocity control, phase modulation, etc.

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REFERENCES