EEMD and bidimensional RLS to suppress physiological interference for heterogeneous distribution in fNIRS study

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Near-infrared spectroscopy (NIRS) can provide the hemodynamics information based on the hemoglobin concentration representing the blood oxygen metabolism of the cerebral cortical, which can be deployed for the cerebral function study. However, NIRS-based cerebral function detection accuracy can be significantly influenced by the physiological activities such as cardiac cycle, respiration, spontaneous low-frequency oscillation and ultra-low frequency oscillation. The distribution difference of the capillary, artery and vein leads to the heterogeneity feature of the cerebral tissues. In the case that the heterogeneity is not serious, good detection accuracy and stable performance can be achieved through the regression analysis as the reference signal can well represent the interference in the measurement signal when conducting the multi-distance measurement approach. The direct use of the reference signal to estimate the interference is not able to achieve good performance in the case that the heterogeneity is serious. In this study, the cerebral function activity signal is extracted using recursive least square (RLS) method based on the multi-distance measurement method in which the reference signal is processed by ensemble empirical mode decomposition (EEMD) algorithm. The temporal and dimensional correlation of the neighboring sampling values are applied to estimate the interference in the measurement signal. Monte Carlo simulation based on a heterogeneous model is adopted here to investigate the
effectiveness of this methodology. The results show that this methodology can effectively suppress the physiological interference and improve the detection accuracy of cerebral activity signal.

Keywords: Ensemble empirical mode decomposition; recursive least square methods; physiological interference; heterogeneous distribution.

1. Introduction

Continuous-wave Near-Infrared spectroscopy (NIRS) which utilizes a constant-frequency or low-frequency modulated diode as the light source has been widely used in obtaining hemodynamic information of oxyhemoglobin, deoxyhemoglobin, etc.\(^1\)\(^-\)\(^3\) The photodiode is often used as the detector. Compared to other cerebral function testing technologies such as electroencephalograph (EEG), magnetoencephalography (MEG), positron emission tomography (PET) and functional magnetic resonance imaging (fMRI), continuous-wave NIRS has shown great capability in various cerebral activity signal detection with advantages of simple construction, low-cost and easily realized miniaturization.\(^4\) However, the detection accuracy of NIRS cerebral function can be significantly influenced by the physiological activities.\(^5\)

In recent years, many international research groups have devoted a great deal of effort to studying physiological interference issues.\(^6\)\(^,\)\(^7\) Physiological disturbances include cardiac cycle, respiration, spontaneous low frequency oscillation, and ultra-low frequency oscillation.\(^8\) The sources of its effects are two-fold. One is the physiological disturbance in the outer cerebral tissue such as the scalp, skull and cerebrospinal fluid. The other is the physiological disturbance in deep cerebral tissue such as cerebral gray matter and white matter.\(^9\) The physiological interferences are therefore also referred to as global disturbances or systemic physiological disturbances.

To deal with this type of interference effectively, the following four solutions have drawn wide attention in the international community: First, based on adaptive filtering approach, the noise effect is suppressed with the help of auxiliary test equipment. For example, the signal that characterizes heartbeat and respiration is collected through the instruments such as blood pressure monitor, respirometer,\(^10\) spirometer, carbon dioxide analyzer and pulse oximeter.\(^11\) The received signal can be used as reference signal to eliminate the disturbance using least mean square algorithm and Kalman filter algorithm. Second, using a prior frequency (cardiac cycle, \(\sim 1\) Hz; respiration, \(\sim 0.25\) Hz; low frequency oscillation, \(\sim 0.1\) Hz), quasi-sinusoidal signal is regarded as the noise component, and the interference is tracked and then removed through the linear adaptive model and Kalman filter algorithm.\(^12\) Third, considering the cerebral function activity has regional characteristics and the physiological interference has global characteristics, subtraction between the measured signals from the active and inactive regions can separate the cerebral function signals from the interference signals. The typical theory includes principal component analysis (PCA)\(^13\) and independent component analysis (ICA).\(^14\) Fourth, the multi-distance measurement method consisting of pairs of light source-detectors is used: the close-separation source-detector pair is used as the reference signal, the far source-detector pair is used to acquire the synthetic signal containing a target signal and the interference, an adaptive filter model\(^15\)\(^,\)\(^16\) is constructed for the inhibition of interference. The above methods inhibit the physiological interference and obtain a good noise suppression effect to a certain extent but pay insufficient attention to the heterogeneity of cerebral tissue.

In 2008, Saager \textit{et al.} studied the heterogeneity of cerebral tissue based on the multi-distance measurement methods.\(^17\) Research shows that 90\% of subjects have the cerebral tissue without serious heterogeneity, while the other 10\% of subjects show significant heterogeneity. At this point, there are some differences in the distribution of capillaries, arteries and veins in different parts of the cerebral tissue, and the traditional stratified cerebral tissue model is ineffective. In the near-infrared cerebral function tests, physiological disturbances come from the different physiological activities, which may have multiple components. When the nonuniformity of cerebral tissue is serious, different physiological activities will lead to different physiological disturbances in different parts.
positions. For this situation, a more viable solution is to separately estimate the different types of interferences. One way is to obtain a reference signal for each physiological disturbance via a blood pressure monitor, a respirometer, etc., and then to track different physiological disturbances using Kalman filtering, but this method requires additional equipments. Another method is to use multiple prior sin/cos signals as the reference signals of physiological interference to estimate the physiological interference by Kalman filtering, but this needs the prior knowledge of the frequency information of the physiological interference of the subjects. However, it is often hard for implementation in practice due to individual differences.

Considering multi-component characteristics of physiological disturbance and the uneven distribution of interfering components, a new method based on multi-distance measurement is proposed to improve the cerebral function detection accuracy. In this study, the near-spacing detector is used to acquire the extra cerebral tissue synthetic signals that are mainly caused by the physiological interference. The far-spacing signals acquired from far-detector are sufficiently sensitive to brain activity. The near channel signal is treated as the reference signal and is decomposed into a series of simple intrinsic mode functions using ensemble empirical mode decomposition (EEMD). The intrinsic mode functions have good instantaneous frequency characteristics and are suitable for nonlinear nonstationary signal analysis. The temporal correlation of neighboring sampling values is studied, and the estimated points are used as the center for smoothing processing. The physiological interference is further estimated using the recursive least square (RLS) algorithm. Monte Carlo simulation results show that this algorithm can effectively inhibit physiological interference and improve the detection accuracy of cerebral activity signal.

2. Theory

2.1. EEMD

Empirical mode decomposition (EMD), as an adaptive time-frequency analysis method, is widely used in biomedical signal processing and is especially suitable for analyzing nonlinear and nonstationary signals. However, there are some shortcomings in the application of EMD. One of the main drawbacks is the existence of serious mode mixing phenomenon in EMD, which leads to receiving different time-scale or similar time-scale information in the intrinsic mode function components. The mode mixing in EMD makes the physical meaning of the individual intrinsic mode function unclear. In order to overcome the mode mixing problems, Huang et al. propose the EEMD by adding a white noise to the original signal. As the white noise distributes uniformly in the whole time-frequency space, the problem of mode mixing can be avoided by adding the white noise signal to make the frequency distribution of the synthetic signal uniform.

Denote the measurement of oxyhemoglobin, deoxyhemoglobin concentration change $x(t)$, white noise series are added with the zero mean and constant variance. The signal is then decomposed into IMFs using EMD. Repeat the same procedure with different white noise series each time and adopt the means of the ensemble corresponding IMFs to avoid the white noise effect to achieve the final IMF components.

$$c_j(k) = \frac{1}{M} \sum_{i=1}^{M} c_{i,j}(t),$$

where $c_j(t)$ is the $j$th IMF component achieved using EEMD. $c_{i,j}(t)$ is the $j$th IMF component by adding white noise series at the $i$th time, $1 \leq i \leq M$.

The final results using EEMD are as follows:

$$x^k(t) = \sum_{i=1}^{N} c_j(t) + r(t),$$

where $r(t)$ is the final residue component describing the signal average trend. $N$ is a positive integer describing the total number of the IMF components using EEMD.

2.2. EEMD-BRLS

The signal $x(k)$ is the $\Delta[HbO_2]$ or $\Delta[HHb]$ acquired from the short-distance measurement S-D1 at instant $k$ and is used to be decomposed for multiple components. The decomposed IMF components are achieved by EEMD. The first dimension is the order $i$ of the EEMD decomposition, which corresponds to time-scales. The larger the value of $i$ is, the smaller the time-scale of the IMF component is. The other dimension is the time series $k$, which indicates the
Fig. 1. Block diagram of global interference denoising using EEMD-BRLS algorithm in multi-distance fNIRS measurement.

signal changes with time. In the previous study, the EMD-RLS algorithm\(^\text{21}\) considers only the relationship between IMF components of different order at the current moment \(k\) and physiological interference and does not take into account that the signals of the adjacent sampling points are correlated.

In order to capture the correlation information in physiological disturbance estimation and achieve better estimation results, we explore the method of EEMD and bidimensional RLS (EEMD-BRLS) by investigating and analyzing the tapped delay line filter. The block diagram of EEMD-BRLS is shown in Fig. 1. For a specific time \(k\), we select the window of length \(2M + 1\) with the time \(k\) as the center. The two-dimensional weight \(w_{i,j}(k)\) as described in Eq. (3) describes the relationship between IMF components and physiological disturbances. This process is similar to smoothing operations in signal processing and is a posterior form of estimation since observed data after the point of interest are used for estimation. As more associated data accumulates around the estimated point, smoothing operation tends to give better estimation than filtering. Here, the estimate of physiological disturbance can be expressed as

\[
\hat{d}(k) = \sum_{i=1}^{N} \sum_{j=-M}^{k+M} w_{i,j}(k)c_i(k-j), \tag{3}
\]

where \(M\) is the half-window size, \(N\) is the decomposition order for EEMD. Equation (3) takes into account the correlation between the IMF order and time, so it is called EEMD-BRLS. The bidirectional weight can be interpreted as the \(i\)th IMF component \(c_i(k)\) passing through an FIR filter of length \(2M + 1\) with coefficient \(w_{i,j}(k)\). Therefore, it is equivalent to a filter bank consisting of \(N\) filters, each of which processes one IMF component and the final result is the sum of the outputs of all the filters. Compared with EEMD-RLS, EEMD-BRLS considers the correlation between adjacent sampling points at the expense of increased computational complexity.

Similar to EEMD-RLS, the cost function is the weighted square sum as follows:

\[
J(k) = \sum_{i=1}^{k} \chi^{k-n} \left[ s(n) - \sum_{i=1}^{N} \sum_{j=k-M}^{k+M} w_{i,j}(k)c_i(k-j) \right]^2.
\tag{4}
\]

The parameter \(0 < \chi < 1\) is the forgetting factor that controls the memory span of the algorithm. Differentiate the equation with respect to \(w_{i,j}(k)\), set it to zero, we can get,

\[
\sum_{i=1}^{N} \sum_{m=k-M}^{k+M} w_{i,m}(k)R_{i,m,j}(k) = p_{i,j}(k),
\quad i = 1, \ldots, N, \quad j = k - M, \ldots, k + M, \tag{5}
\]

where \(R(l,i,m,j)\) and \(p_{i,j}(k)\) are

\[
R_{i,m,j}(k) = \sum_{n=1}^{k} \chi^{k-n}c_i(n-m)c_j(n-j), \tag{6}
\]

\[
p_{i,j}(k) = \sum_{n=1}^{k} \chi^{k-n}s(n)c_i(n-j). \tag{7}
\]
If $(2M + 1)N$ equations are considered, we can get the equation below
\[
\mathbf{R}(k)\mathbf{w}(k) = \mathbf{p}(k),
\]
where
\[
\mathbf{R}(k) = \begin{bmatrix}
R_{1,1,-M,M}(k) & R_{1,1,-M+1,M}(k) & \cdots & R_{1,1,M,M}(k) \\
R_{1,1,-M+1,M+1}(k) & R_{1,1,-M+1,M+1}(k) & \cdots & R_{1,1,M+1,M+1}(k) \\
\vdots & \vdots & \ddots & \vdots \\
R_{1,N-M,M}(k) & R_{1,N-M+1,M}(k) & \cdots & R_{1,N,M,M}(k)
\end{bmatrix},
\]
\[
\mathbf{w}(k) = \begin{bmatrix}
w_{1,-M}(k) \\
w_{1,-M+1}(k) \\
\vdots \\
w_{N,M}(k)
\end{bmatrix},
\]
\[
\mathbf{p}(k) = \begin{bmatrix}
p_{1,-M}(k) \\
p_{1,-M+1}(k) \\
\vdots \\
p_{N,M}(k)
\end{bmatrix},
\]
using Eq. (8), if the $\mathbf{R}(k)$ is not singular, $\mathbf{w}(k)$ can be calculated as
\[
\mathbf{w}(k) = \mathbf{R}^{-1}(k)\mathbf{p}(k).
\]

The dimension of $\mathbf{R}(k)$ is $(2M + 1)N \times (2M + 1)N$. Given $\mathbf{w}(k)$, the cerebral function signal can be extracted based on the matrix inversion lemma.

In the EEMD-BRLS algorithm, a larger $M$ will improve the performance of the estimation because more time-related signals are considered. But once $M$ reaches a certain value, the system performance cannot be improved significantly, even though the amount of computing has increased dramatically. Therefore, in practical application, the half-window length $M$ is selected according to specific system requirement.

### 3. Monte Carlo Simulation

Our study used multi-distance probe arrangement and two wavelengths of the light source (750 nm and 830 nm). A five-layer slab model consisting of scalp (sc), skull (sk), cerebrospinal fluid (csf), gray matter (gm) and white matter (wm) was used as a human adult head model (Fig. 2). We adopt particular source-detector separations to distinguish between processes occurring at different tissue depths, as indicated by the ‘banana-shaped’ regions that encompass statistically determined photon paths. The short separation with source-detector1 is used to probe the superficial tissue layer, and the long distance with source-detector2 to probe the deeper tissue layer. The short source-detector spacing was set to 10 mm and the long source-detector spacing was set to 40 mm. The generation of the NIRS time series was conducted with Monte Carlo simulations and standard analysis of functional hemodynamic changes.

The simulated cerebral function activity process is based on the block design experiment paradigm. The experiment is divided into the Stimu Phase and the Rest Phase (Fig. 3). The Stimu and Rest phases both lasted 20 s and alternated. The entire test time is 200 s. As shown in Fig. 3, sampling rate is 10 Hz, the entire measurement process collects 2000 points of data. For each layer of cerebral tissue, both cardiac cycle and respiratory-induced physiological disturbances are simulated, and the cerebral Stimu Phase is achieved through an increase in HbO2 concentration and a decrease in HHb concentration.

In the process of the simulation, the scattering coefficient of cerebral tissue in each layer is kept constant, and the change of light intensity is determined by the change of absorption coefficient. Therefore, the change of HbO2 and HHb concentration ($\Delta[HbO2]$ and $\Delta[HHb]$) can be calculated with the modified Lambert–Beer law as raw measurements of hemodynamic parameters over time during cerebral functional activity. In order to eliminate the physiological interference, we can
obtain the data of $\Delta[HbO_2]$ and $\Delta[HHb]$ by using the signal extraction method to process the raw data. Since the experimental process is performed using Monte Carlo simulations, the true $\Delta[HbO_2]$ and $\Delta[HHb]$ are pre-known. By comparing the true values, raw measurement data and the extracted values of $\Delta[HbO_2]$ and $\Delta[HHb]$, the validity of the cerebral function signal extraction method can be quantitatively analyzed and compared.

4. Results

Since the consideration of both different orders of IMF component and temporal correlation guarantees the EEMD-BRLS algorithm with high accuracy, we first analyzed the effects of the algorithm in testing cerebral function. Then, targeting the issue of different influences from various physiological activities on reference signal and synthetic signal caused by heterogeneity in the brain, the performances of RLS, EEMD-RLS and EEMD-BRLS algorithms are compared and analyzed using the mean squared errors (MSEs) from statistical results.

Simulation experiment is based on the five-layer cerebral tissue model suggested in earlier studies, and the Monte Carlo simulation program. We utilize the block design experimental paradigm of cerebral function, and take physiological interferences caused by cardiac cycle (frequency of 1.1 Hz), breathing (frequency of 0.18 Hz), low frequency oscillation (frequency of 0.1 Hz), as well as ultra-low frequency oscillation (frequency of 0.04 Hz) into consideration. Physiological interferences are appended to changes in hemodynamics of cerebral tissues, then, white noise with mean value of 0 and 1/100 standard deviation is generated to simulate random noise from actual measurements. Finally, the information of optical density changes is gathered through Monte Carlo simulation. The value of the length of half-window is set as 5 considering the complexity of the algorithm in order to get better simulation results.

Concentration changes of oxyhemoglobin reconstructed with EEMD-BRLS algorithm is shown in Fig. 4. Results are represented in 200 s time series on the left, and the block averages are on the right. Figures 4(a) and 4(b) are acquired with near-separation detector, while Figs. 4(c) and 4(d) are acquired with far-separation detector. Based on the multi-distance measurement and EEMD-BRLS algorithm, changes in oxyhemoglobin concentration as well as the coherent averages are represented in Figs. 4(e) and 4(f). After partial volume effect (PVE) compensation of changes in oxyhemoglobin concentration collected with the EEMD-BRLS algorithm, results and block averages are shown in Figs. 4(g) and 4(h), in which the full line represents extracted value, and the dashed line represents the actual value.

Concentration changes of deoxyhemoglobin reconstructed with EEMD-BRLS algorithm are shown in Fig. 5. Results are represented in 200 s time series on the left, and coherent averages are on the right. Figures 5(a) and 5(b) are acquired with near-end detector, while Figs. 5(c) and 5(d) are acquired with remote detector. Based on multi-distance measurement and EEMD-BRLS algorithm, changes in deoxyhemoglobin concentration as well as the coherent averages are represented in Figs. 5(e) and 5(f). After PVE compensation of changes in deoxyhemoglobin concentration are collected with the EEMD-BRLS algorithm, results and coherent averages are shown in Figs. 5(g) and 5(h), in which the full line represents extracted value, and the dashed line represents the actual value.

Observing Figs. 4 and 5, we noticed that there is obvious physiological interference of synthetic signals in Figs. 4(a) and 4(c), as well as in Figs. 5(a) and 5(c), along with their block averages. Extracted changes in hemodynamic parameters and actual changes in hemodynamics are quite close from
Figs. 4(g) and 4(h), as well as Figs. 5(g) and 5(h). From these results, we knew that utilizing the EEMD-BRLS algorithm based on multi-distance measurement could suppress physiological interferences and effectively extract cerebral function signals.

Under normal conditions, heterogeneity of hemodynamic parameters in extracerebral tissues and deep cerebral cortex is not severe, thus adaptive filtering based on multi-distance measurement can reduce physiological interference very effectively. Saager et al. use both linear and circular light source-detector layouts to study the heterogeneity of local cerebral tissues, and observed obvious heterogeneity in the cerebral tissues in 10% of testers. Considering the fact that degree of disturbance on different cerebral regions is distinct from diverse physiological activities because of the heterogeneity in cerebral tissues, percentage of various physiological activities in reference signal and synthetic signal is changed during simulation. Since the effects from different interferences are similar, we will only study the example of heartbeat interference. Although heartbeat is global physiological interference, heterogeneity of cerebral tissues resulted from differences in the volume, distribution and shape of blood vessels could lead to nonuniform influences by heartbeat on different regions. Focusing on control parameters in previous studies, we assume that disturbance by heartbeat in the region detected by near-separation optical detector is significantly larger than that in any other region, and the exceeding amount is measured in percentage. Zero percent represents the same amount of heartbeat interference compared to other tissues, which means homogeneity, while 100% means the interference from heartbeat in this region is one-fold higher than other tissues, and the heterogeneity is severe.

During Monte Carlo simulation, control parameters of physiological disturbance amplitudes among different tissues (amplitude control parameters) are valued with 20% intervals, and the MSE is obtained by taking the average of 100
independent experiments. The simulation results are shown in Fig. 6, where Fig. 6(a) contains the MSE of concentration changes of oxyhemoglobin, and Fig. 6(b) contains the MSE of concentration changes of deoxyhemoglobin. From Fig. 6(a), we conclude from the MSE value that the RLS algorithm could most accurately perform cerebral function detection while the amplitude control parameter remain unchanged (cerebral tissues have ideal homogeneity). When the amplitude control parameter increases (tissues begin to show severe heterogeneity), the effectiveness of RLS algorithm deteriorates; however, it does not affect EEMD-RLS or EEMD-BRLS algorithm significantly, showing the great robustness of the latter two algorithms. Decomposing reference signals, assigning different values to various IMF components, and adjusting weights self-adaptively, where unrelated IMF components are assigned with small weights and large weights are assigned to strongly related components, these characteristics of the EEMD earned better interference estimations for the algorithm. During optimization, EEMD-BRLS took the relevance of adjacent time of each IMF component into consideration, and used smoothing to process algorithms, thus the MSE calculated with EEMD-BRLS is significantly smaller than that with EEMD-RLS algorithm. Considering Fig. 6(b), the trend of RLS algorithm is similar to that in Fig. 6(a), and EEMD-BRLS algorithm also performed better than the EEMD-RLS algorithm. Compared to the results of changes in concentration of oxyhemoglobin, RLS algorithm performed very well compared to the other two EEMD methods when the change in amplitude control parameters is less than around 45% in the deoxyhemoglobin result. There are two reasons for this phenomenon, the first is that physiological interference has smaller amplitudes for the detection of oxyhemoglobin, which means heterogeneity has far less effect on the detection of change in concentration of oxyhemoglobin than that on deoxyhemoglobin; secondly, although EEMD decomposition can provide intrinsic mode functions of different simple components,
fluctuations may occur during decomposition process, and could bring errors to the ultimate optimization results. Thus, when the tissue heterogeneity is not severe, advantages of EEMD-RLS and EEMD-BRLS algorithms could not offset the fluctuations during EEMD decomposition and could lead to results worse than the RLS algorithm.

To analyze the performance of EEMD-BRLS algorithm with different half-window lengths, statistical analyses are performed on MSEs when half-window length ($M$) ranged from 1 to 5, and the result is shown in Fig. 7. Corresponding MSE values with alternating concentrations of oxygenated and deoxyhemoglobin are plotted in Figs. 7(a) and 7(b), respectively. Similar conclusions are drawn from both figures, the larger the $M$ is, the smaller the MSE value is, which means the better results are obtained when half-window length is large. However, large $M$ values do not necessarily mean good results. Our simulation results showed that when $M$ is larger than 5, the trend for smaller MSE value slows down, and when $M$ is larger than 8, MSE does

Fig. 6. MSE versus the variation of amplitude control parameters for three different algorithms. (a) The MSE of concentration changes of oxyhemoglobin and (b) the MSE of concentration changes of deoxyhemoglobin.

Fig. 7. Performance comparations of EEMD-BRLS in different half-window length $M$. (a) The MSE of concentration changes of oxyhemoglobin and (b) the MSE of concentration changes of deoxyhemoglobin.
not significantly decrease. Overall, considering the complexity of algorithms, when studying the extraction of cerebral function signals, half-window length of 5 is the most appropriate, and MSE value increases along with the increase in amplitude control parameters; however, EEMD-BRLS algorithm has better robustness compared to RLS algorithm.

5. Discussion

Physiological interference can greatly degrade the performance of fNIRS measurement of evoked brain activity response. Many different methodologies have been explored to resolve this problem. One of the approaches is to identify and separate the interference components in fNIRS study including using auxiliary physiological measurements and to analyze the signal with an adaptive filtering algorithm. The instruments such as electrocardiogram (ECG), the pulse oximeter, chest band respirometer, spirometer and capnograph can be used to achieve auxiliary physiological measurements. This method has the drawback of the indispensability of additional equipment. Another approach adopted adaptive filtering methods to separate the brain activity response and the physiological interference using the priori frequencies. The priori frequencies (e.g., the cardiac, ∼1 Hz; respiratory, ∼0.25 Hz; and Mayer wave frequency, ∼0.1 Hz) have also been assumed to be the sine/cosine terms. However, this methodology is not appropriate due to individual difference. Thus, recently multi-distance measurement and adaptive filtering have been proposed to suppress the physiological interference and the advantage of this method is convenient and effective to extract the signal for real-time application.

It should be noted that in the multi-distance measurement method, the performance of adaptive filtering declines due to heterogeneous problem. In this current paper, we employ the time-frequency analyzing method to decompose the reference signal and then using RLS algorithm to estimate the brain activity response. The accuracy of the EEMD-RLS algorithm and EEMD-BRLS algorithm depends on the reference signal decomposition. Therefore, this paper uses the improved EMD algorithm EEMD to improve the accuracy of the decomposition. In addition, the EEMD-RLS and EEMD-BRLS algorithms have no obvious differences when the tissue heterogeneity is not serious, while the RLS algorithm is easy to implement and can be utilized for real-time signal processing without EEMD processing procedure. The EEMD-RLS and EEMD-BRLS algorithms can significantly improve system robustness when the distributions of disruptions caused by different physiological activities in different regions are not consistent.

An important matter that should be considered here is the EEMD-RLS and EEMD-BRLS algorithms can not only conduct the cerebral function signals detection, but also provide the extracerebral hemodynamic changes for cerebral function study as they can provide the time-frequency information of the outer layer of the brain via EEMD. During the cerebral stimulation, the hemodynamic parameters of extracerebral layers are not always independent of the response to the cerebral cortex. For example, the cardiac cycle increase during finger motility experiments increases hemodynamic correlations between the outer layer of the cerebral and the cerebral cortex, which may lead to over-fitting in cerebral function testing via multiple-range measurements. The cerebral function signals can be extracted by EEMD-RLS and EEMD-BRLS approaches. At the same time, the information of frequency components regarding the outer layers of cerebral tissue can be achieved via EEMD method to further analyze the hemodynamics of the outer layer of cerebral tissue.

A truly rigorous evaluation of this method requires the simulation of the heterogeneous head model, which unfortunately, is not easy to realize for the in vivo experiments as such experiments need the selection of the heterogeneous subjects. Meanwhile, the PVE effect in vivo cannot be exactly compensated and the quantitative comparison of the recovery response and the true response of brain activity is difficult. Thus, the control parameters are altered with fixed steps to imitate the heterogeneous head tissue. Monte Carlo simulation is further implemented for quantitative analysis here as the preliminary study. As for the deep study of this method in vivo with practical NIRS measurement, this will be the subject of our on-going research and will be published in due course.

6. Conclusions

In this paper, multi-distance measurement method has been investigated regarding eliminating the
physiological interference for cerebral function signals detection. An EEMD-BRLS algorithm is proposed based on the EEMD optimization. Considering the temporal correlation of the neighboring sampling values, the EEMD-BRLS algorithm is obtained by performing the smoothing operation centered on the estimated points. The results of EEMD-BRLS algorithm are analyzed based on a five-layer tissue model and Monte Carlo simulation. In addition, considering the heterogeneity of cerebral tissue, RLS adaptive filtering, EEMD-RLS and EEMD-BRLS algorithms are compared, respectively, by adjusting the different proportions of various interferences in the reference signal and the expected signal. The simulation results show that EEMD-BRLS algorithm and EEMD-RLS algorithm have higher estimation accuracy than RLS algorithm, and EEMD-BRLS is superior to EEMD-RLS algorithm when various interferences have different proportions in reference signal and expected signal.

**Conflicts of Interest**

The authors declare that they have no conflicts of interest.

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**References**


