做科研，非一朝一夕
---买器材，应速战速决

Newport数千种优质产品当日发货，
更多惊喜尽在PhotonSpeed™光速购！
Layer-modulated two-photon absorption in MoS$_2$: probing the shift of the excitonic dark state and band-edge

Yafeng Xie,1,2 Saifeng Zhang,1,6 Yuanxin Li,1 Ningning Dong,1 Xiaoyan Zhang,1 Lei Wang,1,2 Weimin Liu,3 Ivan M. Kislyakov,1 * Jean-Michel Nunzi,1,4 Hongji Qi,1 Long Zhang,1 and Jun Wang1,2,5,*

1Laboratory of Micro-Nano Optoelectronic Materials and Devices and CAS Key Laboratory of Materials for High-Power Laser, Shanghai Institute of Optics and Fine Mechanics, Chinese Academy of Sciences, Shanghai 201800, China
2Center of Materials Science and Optoelectronics Engineering, University of Chinese Academy of Sciences, Beijing 100049, China
3School of Physical Science and Technology, ShanghaiTech University, Shanghai 201210, China
4Department of Physics, Engineering Physics & Astronomy and Department of Chemistry, Queen’s University, Kingston, Ontario K7L-3N6, Canada
5State Key Laboratory of High Field Laser Physics, Shanghai Institute of Optics and Fine Mechanics, Chinese Academy of Sciences, Shanghai 201800, China
6E-mail: sfzhang@siom.ac.cn
*Corresponding author: jwang@siom.ac.cn

Received 7 December 2018; revised 7 April 2019; accepted 15 April 2019; posted 2 May 2019 (Doc. ID 354796); published 19 June 2019

Questions hovering over the modulation of bandgap size and excitonic effect on nonlinear absorption in two-dimensional transition metal dichalcogenides (TMDCs) have restricted their application in micro/nano optical modulator, optical switching, and beam shaping devices. Here, degenerate two-photon absorption (TPA) in the near-infrared region was studied experimentally in mechanically exfoliated MoS$_2$ from single layer to multilayer. The layer-dependent TPA coefficients were significantly modulated by the detuning of the excitonic dark state (2p). The shift of the quasiparticle bandgap and the decreasing of exciton binding energy with layers were deduced, combined with the non-hydrogen model of excitons in TMDCs and the scaling rule of semiconductors. Our work clearly demonstrates the layer modulation of nonlinear absorption in TMDCs and provides support for layer-dependent nonlinear optical devices, such as optical limiters and optical switches.

1. INTRODUCTION

Layered transition metal dichalcogenides (TMDCs) exhibit unique nonlinear optical (NLO) properties, including high-order harmonic generation, ultrafast saturable absorption, optical limiting, multi-photon absorption, and so on [1–5]. Intrinsically, mono- and few-layered TMDCs possess large excitonic effects. Recently, the existence of excitonic dark states in monolayers (MLs) WS$_2$ and MoS$_2$ has been revealed via two-photon photoluminescence (TPL) spectroscopy, demonstrating their potential application in optoelectronic and quantum devices [6–9]. However, it should be noted that the TPL technique is applicable only to photoluminescent materials, whereas most TMDCs, especially multilayered ones, are with low-quantum-yield or nonluminous, hampering the investigation of layer modulation (essentially excitonic dark state modulation) on the NLO absorption of TMDCs. In this work, we probed the degenerate two-photon absorption (TPA) of two-dimensional (2D) MoS$_2$ directly utilizing an NLO intensity scan setup (micro-I-scan) for micro/nano materials [10,11]. The TPA coefficients of MoS$_2$ ranging from ML to 31 layers (31L) were obtained, which were deeply modulated by the detuning of the excitonic dark state. Using a non-hydrogen model in combination with the scaling rule of semiconductors [12], the shift of the quasiparticle bandgap and the excitonic dark state with van der Waals layers were deduced [13–15]. In addition, the sub-band resonance in the conduction band was also observed in multilayer MoS$_2$.

2. MATERIALS AND CHARACTERIZATION

Layered MoS$_2$ nanosheets were mechanically exfoliated from the bulk crystal [16,17], and then transferred to a quartz substrate, which would affect the light absorption extremely weakly [18,19]. As shown in Fig. 1(a), the morphology of the samples can be readily identified using a 50× objective lens. The lateral
size of the samples was determined to be 10 to 100 μm, which is suitable for our NLO measurements. Raman spectroscopy and photoluminescence (PL) spectroscopy were performed, shown in Fig. 1. Both the Raman and PL signals were collected using a confocal microscopy setup (Horiba Co., HR Evolution) with a green continuous-wave (CW) laser at 532 nm (∼1.3 kW/cm² at focus). The exact thickness of all samples was measured using atomic force microscopy (AFM). Figure 1(b) shows the thickness of the mono- and bilayer MoS₂. Additional AFM images are provided in the Appendices (Fig. 8).

As shown in Fig. 1(f), two Raman-active modes, E₂g and A₁g, exhibit significant layer dependence. The Raman shifts of mono-, bi-, and trilayers are ∼18.99 cm⁻¹, ∼21.98 cm⁻¹, and ∼23.71 cm⁻¹, respectively, which are consistent with previous literature results [4,20]. In addition, the two Raman vibration modes provide strong evidence that all the samples used in our work are 2H-MoS₂ [4,21]. The PL spectra of MoS₂ were obtained under the same incident power. As shown in Fig. 1(c), there are two peaks at 670 nm and 615 nm corresponding to the A and B excitonic (1s) ground states, which come from energy splitting (∼150 meV) near the valence-band maximum due to spin-orbit coupling [22–25]. The linear absorption spectra were achieved using a confocal microscope, which are plotted in Fig. 1(e). It should be noted that there is a slight shift of the two distinct excitonic absorption peaks with layer number, but the strong excitonic effect still exists.

3. RESULTS AND DISCUSSION

A. Two-Photon Absorption Properties

The TPA process in layered MoS₂ was investigated using a micro-I scan setup [10], which integrates a microscopic imaging system (Fig. 10). The femtosecond laser pulses (pulse width: 340 fs, repetition rate: 1 kHz) at 1030 nm (1.204 eV) were generated from a mode-locked fiber laser. The laser beam was finally focused down to a spot with a waist radius w_p of ∼5 μm on the surface of the MoS₂ (Fig. 7). The intensity of the incident pulses was adjusted continuously with a linearly adjustable attenuator. The process that accounts for one- and two-photon absorption can be described by the propagation equation [2,10,11,26–29]:

\[
\frac{dl(z)}{dz} = -\alpha l - \beta(I) I^2(z). \tag{1}
\]

Here, z is the propagation distance of the laser beam in the sample. \(\alpha\) is the one-photon (linear) absorption coefficient, which cannot contribute to the total absorption significantly owing to the smaller value of the photon energy of 1.2 eV than the optical bandgap [30–32]. \(\beta(I)\) is the TPA coefficient. In our experiment, the excitation laser source was a series of Gaussian pulses, i.e.,

\[
I(r, t) = I_0 \cdot \exp \left(-\frac{2r^2}{w_p^2}\right) \cdot \exp \left(-\frac{t^2}{\tau_p^2}\right), \tag{2}
\]

where \(w_p\) and \(\tau_p\) represent the radius of the pump beam waist and the pulse width, respectively.

Compared with previous research on CdS nanocrystals [33], MoS₂ nanosheets have a uniform surface morphology with few defects in such a single crystal. Therefore, the homogeneously broadened saturation model of TPA was taken into account as follows [34,35]:

\[
\beta(I) = \frac{\beta_0}{1 + (I/I_{sat})^\gamma}, \tag{3}
\]

where \(I_{sat}\) is the saturation intensity of TPA. Based on this model, the numerical fitting curves are shown in Fig. 2(a), which agree well with the experimental results (Fig. 9). The TPA coefficients of the layered MoS₂ were extracted, and the detailed parameters are given in Table 1 in the Appendices. As shown in Fig. 2(b), monolayer MoS₂ exhibits the largest TPA coefficient, which declines rapidly until approximately four layers. After that, the TPA coefficient gradually increases with layer number. This anomalous tendency reveals the switching of the optical transition from the excitonic type to the interband one, which will be discussed in the following section.

Due to the 2D geometry of monolayer MoS₂ and poor dielectric screening, the ground-state excitons are well confined with a binding energy of ∼0.63 eV [25]. This is much larger than that of traditional semiconductors and quantum wells (dozens of meV) [36,37]. As shown in Figs. 1(d) and 1(e), the PL and absorption peaks indicate that the A exciton ground state energy level (1s) of all layered MoS₂ is almost the same, with a value of approximately 1.85–1.88 eV. However, the quasiparticle bandgap \(E_g\) is much larger than the optical one according to theoretical predictions [38]. For example, \(E_g\) is about 2.7 eV for the monolayer [25] and 2.427 eV for the bilayer [38]. Moreover, Qiu et al. have theoretically predicted that there are several excitonic dark states between 1.88 eV and 2.7 eV in monolayer MoS₂. According to the transition selection rules, one-photon excitation couples states of opposite parity, as opposed to TPA, which couples states of identical parity [6]. One-photon can excite an electron only to the excitonic ground state (1s) or any other higher-order bright excitonic states. Considering the valley polarization or different valleys in MoS₂, we note that there exists the valley-selective circular dichroism arising from its unique symmetry. However, in our experiment,
we used a linear polarization excitation source rather than a circular one. Both valleys ($K'$ and $K''$) will be populated. In the meanwhile, the valley polarization is obvious only at low temperature. For example, Cao et al. measured the circularly polarized PL of monolayer MoS$_2$ ($P \approx 50\%$) at 83 K [39], Zeng et al. gave $P \approx 32\%$ at 10 K [40], and Mak et al. confirmed that at 14 K [41]. We did the TPA measurements at room temperature (about 300 K), at which the phonon-assisted inter-valley scattering becomes important and the valley polarization effect becomes very weak and can be neglected [42]. Hence, the TPA technique is the most effective method to study 2p excitonic dark state transition in mono- and few-layer MoS$_2$. In multilayer MoS$_2$, the red shift of quasiparticle bandgap continues to increase and so do the high excited excitonic states, which leads to a large detuning between 2p excitonic dark state and two-photon excitation [38,43]. Thus, the TPA coefficient can be modulated by the on–off resonance. In addition, it has been calculated that the transition matrix elements for direct transitions would vary with the number of layers. However, the matrix element at the $K$ point is always the strongest position [44,45].

B. Theoretical Analysis

In 2D, the hydrogen model employs an effective mass Hamiltonian $H = -\hbar^2\nabla^2/2\mu + V_{ch}(r)$, where $V_{ch}(r) = -\epsilon^2/4\pi\epsilon_r$ is locally screened attractive electron–hole interaction. Depending on this model, the excitonic energy level in TMDCs can be calculated using Eq. (4) [46]:

$$E_{n}^{(a)} = \frac{\mu e^4}{2\hbar^2\epsilon_r^2 \left( n - \frac{1}{2} \right)^2} = E_g - E_n,$$  \hspace{1cm} (4)

where $E_{n}^{(a)}$ is the binding energy of the $n$ exciton state, $E_g$ is the quasiparticle bandgap, $E_n$ is the $n$th-order excitonic energy level, and $n$ is the excitonic principal quantum number. However, the description of 2D excitons is complicated by the fact that the screening cannot be assumed to be local. Therefore, Chernikov et al. considered a nonlocally screened electron–hole interaction described by the potential $V_{ch}(r) = -\epsilon^2/4\pi\epsilon_r \left[ H_0(\epsilon^2 r) - Y_0(\epsilon^2 r) \right]$, where $H_0$ and $Y_0$ are Struve and Bessel functions, and numerically calculated the radially symmetric excitonic Hamiltonian. From another point of view, the dielectric screening parameter is no longer a constant, which should be an $n$-dependent value. The analytical expression for the nonlocal 2D screening depends on the excitonic mass and 2D polarizability [15]:

$$\epsilon_{n} = \frac{1}{2} \left[ 1 + \sqrt{1 + \frac{32\pi a\mu}{9n(n - 1) + 3}} \right].$$  \hspace{1cm} (5)

Here, $\mu = 1/(m_e^{-1} + m_h^{-1})$ is the exciton reduced mass, $\alpha$ is the 2D polarizability, the internal polarizability of the 2D dielectric [15,47], and $\epsilon_{n}$ is the $n$-dependent effective screening dielectric parameter.

Combining Eqs. (4) and (5), we can obtain the $n = 2$ energy levels of the A-excitonic state (2s) of monolayer and bilayer, which are 2.412 eV and 2.175 eV, respectively. The detail of the calculation can be found in the Appendices. It is worth

---

**Table 1. Complete Parameters of Thickness and NLO Coefficients**

<table>
<thead>
<tr>
<th>Sample</th>
<th>Thickness (nm)</th>
<th>TPA Coefficient ($\beta_0$) ($10^3$ cm/GW)</th>
<th>Saturation Intensity ($I_{sat}$) ($10^2$ GW/cm$^2$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>ME-1L</td>
<td>$\sim 0.7$</td>
<td>1.88 ± 0.21</td>
<td>1.98 ± 0.16</td>
</tr>
<tr>
<td>ME-2L</td>
<td>$\sim 1.4$</td>
<td>0.38 ± 0.15</td>
<td>2.05 ± 0.24</td>
</tr>
<tr>
<td>ME-3L</td>
<td>$\sim 2.1$</td>
<td>0.25 ± 0.13</td>
<td>2.59 ± 0.13</td>
</tr>
<tr>
<td>ME-4L</td>
<td>$\sim 3.0$</td>
<td>0.19 ± 0.12</td>
<td>4.28 ± 0.28</td>
</tr>
<tr>
<td>ME-7L</td>
<td>$\sim 5.0$</td>
<td>0.46 ± 0.16</td>
<td>2.52 ± 0.24</td>
</tr>
<tr>
<td>ME-9L</td>
<td>$\sim 6.3$</td>
<td>0.54 ± 0.17</td>
<td>2.19 ± 0.21</td>
</tr>
<tr>
<td>ME-12L</td>
<td>$\sim 8.4$</td>
<td>0.62 ± 0.20</td>
<td>0.97 ± 0.15</td>
</tr>
<tr>
<td>ME-14L</td>
<td>$\sim 9.8$</td>
<td>0.57 ± 0.32</td>
<td>1.27 ± 0.16</td>
</tr>
<tr>
<td>ME-18L</td>
<td>$\sim 11.9$</td>
<td>1.28 ± 0.26</td>
<td>1.82 ± 0.17</td>
</tr>
<tr>
<td>ME-25L</td>
<td>$\sim 16.8$</td>
<td>1.81 ± 0.35</td>
<td>1.18 ± 0.18</td>
</tr>
<tr>
<td>ME-29L</td>
<td>$\sim 20.3$</td>
<td>1.80 ± 0.39</td>
<td>0.42 ± 0.12</td>
</tr>
<tr>
<td>ME-31L</td>
<td>$\sim 21.7$</td>
<td>1.83 ± 0.28</td>
<td>0.70 ± 0.15</td>
</tr>
</tbody>
</table>

---

**Fig. 2.** (a) Micro-I-scan results for monolayer, few-layer, and multilayer MoS$_2$, which are fitted using the homogeneously broadened TPA model. (b) TPA coefficients of layered MoS$_2$. The green solid circle stands for the TPA coefficients, which can be separated into two parts: the trailing edge (as indicated by the blue solid line) corresponds to the excitonic resonance part, and the following rising edge corresponds to the interband transition part. The orange dashed line indicates the transition of MoS$_2$ from the two-dimensional prototype to the bulk one.
As the thickness of MoS$_2$ is increased from a single layer to multilayers, the interaction between the van der Waals layers gets stronger, and both the quasiparticle bandgap and the binding energy of the excitons decrease [38]. Consequently, when the quasiparticle bandgap is less than 2.4 eV, TPA can occur from the valence band to conduction band. In this case, the quasiparticle bandgap can be estimated by the scaling rule applicable to most semiconductors, including multilayer TMDCs [54–57]:

$$
\beta_0 = \frac{K \sqrt{E_g} F(2\hbar \omega/E_g)}{n_0 E_g^3},
$$

where $K$ is a material-independent constant, $n_0$ is the linear refractive index of the material, and $E_g$ (related to the Kane momentum parameter) is nearly material independent for a wide variety of semiconductors. By taking parabolic bands near the $K$ point in the first Brillouin zone into consideration, the function $F$ is given by [54]

$$
F(2\hbar \omega/E_g) = (2\hbar \omega/E_g - 1)^{3/2}/(2\hbar \omega/E_g)^3.
$$

$E_g$ is about 21 eV, the same order of magnitude as previous results [54,55,58]. $K$ is about $10^6$, larger than that of traditional semiconductors [56], implying strong exciton effect in TMDCs. It can be seen in Fig. 2(b) that $\beta_0$ gradually reaches a constant value when the layer number increases to about 25. It indicates that layered MoS$_2$ with such thickness has a similar TPA performance as the bulk, i.e., they are substantially bulk MoS$_2$.

Fig. 3. Schematic illustration of a TPA-active exciton at the $K$ point in the Brillouin zone. 1s and 2p (~1.88 eV and ~2.41 eV in monolayer MoS$_2$) represent ground state and the first excitonic dark state in a 2D non-hydrogen model. (a) In monolayer MoS$_2$, the 2p excitonic dark state is almost in resonance with two-photon energy. (b) In few-layer MoS$_2$, the excitonic resonance detuning increases with layer number. (c) In multilayer MoS$_2$, the red shift of quasiparticle bandgap continues to increase, and the interband TPA occurs.

Fig. 4. Shift of the quasiparticle bandgap $E_g$ and the first excited excitonic state ($E_{2\text{p}-1}$) versus number of layers. As a result, the exciton binding energy ($E_b^{1\text{-exc}}$ and $E_b^{2\text{-exc}}$) decreases with layer number (bottom inset). The 1s-excitonic state locates at ~1.88 eV [obtained from the linear absorption spectra in Fig. 1(e)] and is independent of the layer number Here. $n$ is the principal quantum number in the non-hydrogen model. Top inset: increase of the dielectric parameter ($\varepsilon_3^{\text{ref}}$, $\varepsilon_3^{\text{cal}}$) with layers. The dashed lines are intended as a visual guide.
Table 2. Dielectric Parameters ($\varepsilon_{n=1}$, $\varepsilon_{n=2}$), Quasiparticle Bandgap $E_g$, Energy Level, and Binding Energy for $n = 1$ and $n = 2$ Excitonic States from Monolayer to Multilayer

<table>
<thead>
<tr>
<th>Layers</th>
<th>$\varepsilon_{n=1}$</th>
<th>$\varepsilon_{n=2}$</th>
<th>$E_g$ (eV)</th>
<th>$E_{n=1}$ (eV)</th>
<th>$E_{n=2}$ (eV)</th>
<th>$E_b^{n=1}$</th>
<th>$E_b^{n=2}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>2.8</td>
<td>1.49</td>
<td>2.759</td>
<td>1.88</td>
<td>2.412</td>
<td>0.879</td>
<td>0.347</td>
</tr>
<tr>
<td>2</td>
<td>3.55</td>
<td>1.74</td>
<td>2.427</td>
<td>1.86</td>
<td>2.175</td>
<td>0.567</td>
<td>0.252</td>
</tr>
<tr>
<td>3</td>
<td>3.96</td>
<td>1.89</td>
<td>2.319 ± 0.022</td>
<td>N.A.</td>
<td>2.105</td>
<td>N.A.</td>
<td>0.214</td>
</tr>
<tr>
<td>4</td>
<td>3.90</td>
<td>1.86</td>
<td>2.333 ± 0.020</td>
<td>N.A.</td>
<td>2.113</td>
<td>N.A.</td>
<td>0.220</td>
</tr>
<tr>
<td>7</td>
<td>4.16</td>
<td>1.96</td>
<td>2.278 ± 0.021</td>
<td>1.85</td>
<td>2.079</td>
<td>0.428</td>
<td>0.199</td>
</tr>
<tr>
<td>9</td>
<td>4.23</td>
<td>1.98</td>
<td>2.264 ± 0.022</td>
<td>N.A.</td>
<td>2.069</td>
<td>N.A.</td>
<td>0.195</td>
</tr>
<tr>
<td>12</td>
<td>4.31</td>
<td>2.01</td>
<td>2.251 ± 0.025</td>
<td>1.88</td>
<td>2.062</td>
<td>0.371</td>
<td>0.189</td>
</tr>
<tr>
<td>14</td>
<td>4.26</td>
<td>1.99</td>
<td>2.259 ± 0.036</td>
<td>N.A.</td>
<td>2.066</td>
<td>N.A.</td>
<td>0.193</td>
</tr>
<tr>
<td>18</td>
<td>5.00</td>
<td>2.26</td>
<td>2.155 ± 0.030</td>
<td>1.85</td>
<td>2.005</td>
<td>0.305</td>
<td>0.150</td>
</tr>
<tr>
<td>25</td>
<td>5.62</td>
<td>2.49</td>
<td>2.098 ± 0.042</td>
<td>1.88</td>
<td>1.975</td>
<td>0.218</td>
<td>0.123</td>
</tr>
<tr>
<td>29</td>
<td>5.60</td>
<td>2.48</td>
<td>2.099 ± 0.046</td>
<td>N.A.</td>
<td>1.976</td>
<td>N.A.</td>
<td>0.124</td>
</tr>
<tr>
<td>31</td>
<td>5.64</td>
<td>2.50</td>
<td>2.096 ± 0.033</td>
<td>N.A.</td>
<td>1.974</td>
<td>N.A.</td>
<td>0.122</td>
</tr>
<tr>
<td>Bulk</td>
<td>5.60</td>
<td>2.48</td>
<td>2.099</td>
<td>1.88</td>
<td>1.976</td>
<td>0.219</td>
<td>0.123</td>
</tr>
</tbody>
</table>

*From Ref. [38].

Combining Eqs. (7) and (8), the relationship between $E_g$ and layer number was obtained for the multilayer MoS$_2$, as shown in Fig. 4. Then the exciton ground state $E_{n=1}$ and first excited state $E_{n=2}$ can be determined using Eq. (5). The corresponding excitonic dark state $E_{2p}$ in a multilayer can be approximately marked by $E_2$ (i.e. $E_{2b}$), neglecting the slight difference (smaller than 0.05 eV) [49]. The shift of the conduction band-edge (corresponding to quasiparticle bandgap $E_g$) and the 2p dark state of A exciton (adjacent to $E_{2b}$) is clearly demonstrated in Fig. 4. The energy distance between $E_2$ and $E_1$ becomes gradually smaller, meaning that the high excitonic states are compressed and the binding energy weakens when layer number increases. The full set of the parameters, $\varepsilon_{n=1}$, $\varepsilon_{n=2}$, $E_g$, and $E_{n=2}$, from monolayer to multilayer are summarized in Table 2. The increasing tendency of the dielectric parameter with layer number is obvious, which implies an increase of the dielectric screening potential. The quasiparticle bandgap $E_g$ and $E_{2b}$ drop to almost a constant when the layer number increases to 25, which is evidence of the transition from 2D to bulk.

To further confirm the excitonic energy compression and the shift of the conduction band-edge, we investigated the excitation photon energy-dependent TPA process in ~25L MoS$_2$, which can be treated as a bulk semiconductor. A wavelength-tunable femtosecond system (35 fs, 1 kHz, TOPAS, Coherent Co.) pumped by a Ti:sapphire laser at 800 nm was used for these measurements. As shown in Fig. 5, the TPA coefficient approximately increases with the excitation photon energy, in good agreement with the scaling rule in Eq. (7). We noticed that there is a distinct peak at about 1.21 eV. Since the quasiparticle bandgap $E_g$ of 25L MoS$_2$ is below 2.1 eV as given in Table 2, TPA (at photon energy ~2.42 eV) of the electrons in the valence band can transit deep into the conduction band; this peak was ascribed to the sub-band resonance [59].

**4. CONCLUSION**

In summary, we prepared monolayer, few-layer, and multilayer MoS$_2$ nanosheets through mechanical exfoliation. Using the micro-I-scan technique, we studied the TPA properties in 2D layered MoS$_2$ and found that the TPA coefficient decreased rapidly from monolayer to few-layer, and increased gradually from few-layer to multilayer up to 25 layers. Combining the non-hydrogen model of excitons in TMDCs with the scaling rule in semiconductors, we deduced the red shift of the 2p excitonic dark state and the band-edge of conduction band with increasing layer number. The quasiparticle bandgap and excitonic dark levels, as well as the binding energy of the exciton dark state dropped dramatically until the layer number increased to 25L, which implies this is the 2D-to-bulk transition point. The sharp decline of the TPA coefficient from monolayer to 2L–4L was ascribed to the on–off resonance of 2p excitonic dark states. In addition, the sub-band resonance in the conduction band was demonstrated. Our results provide valuable insights into the mechanism of the evolution of band structure and excitonic levels in layered MoS$_2$, which can be applied to other TMDCs.
APPENDIX A

In our TPA measurement, the femtosecond pulses centered at 1030 nm are generated from a mode-locked fiber laser. The pulse width is about 10 nm, i.e., the spectral width is \( \sim 10 \text{ meV} \), which is measured using the PG2000 (Ideaoptics) fiber optic spectrometer (see Fig. 6). It is much narrower than that of a Ti:sapphire femtosecond laser. Therefore, resonance excitation should occur between the conduction band maximum (CBM) and the excited excitonic state.

APPENDIX B

In monolayer, the first-order effective screening is given by Ref. [38] in the text:

\[
E_b^{(1)} = \varepsilon_{g} - \varepsilon_{n=1} = 2.759 - 1.88 = 0.879 \text{ eV}, \quad \varepsilon_1 = 2.8,
\]

\[
E^{(\omega)} = \frac{\mu e^4}{2\hbar^2 \varepsilon_n^2 (n - \frac{1}{2})^2}.
\] 

(B2)

Combined with Eqs. (B1) and (B2), we can get that \( \varepsilon_2 = 1.49 \) and \( E_b^{(2)} = 0.347 \text{ eV} \).

Meanwhile, we can obtain the value of \( \alpha \mu \) of \( \sim 0.60 \), and \( \frac{\mu e^4}{2\hbar^2} \) of \( \sim 1.72 \text{ eV} \), which are assumed as constants in few-layer and multilayer MoS\(_2\). Hence, we can calculate the \( \varepsilon_1, \varepsilon_2, \) and \( E_b^{(2)} \) of few-layer and multilayer MoS\(_2\), as shown in Table 2. 

Fig. 6. Spectrum of the femtosecond laser pulse in the nonlinear optical measurements.

Fig. 7. Identification of the size of laser beam spot in our nonlinear optical measurements; the radius is \( \sim 5 \mu\text{m} \).
Fig. 8. AFM images of few-layer and multilayer MoS$_2$.

Fig. 9. Complete micro-I-scan fitting results of monolayer, few-layer, and multilayer MoS$_2$, according to the homogeneously broadened TPA model.

Fig. 10. Schematic diagram of the setup of micro-intensity scan.
Acknowledgment. The authors acknowledge the utilization of equipment in the School of Physical Science and Technology in ShanghaiTech University. Y. F. Xie is grateful for the detailed discussion with Prof. Jean-Michel Nunzi.

Disclosures. The authors declare that there are no conflicts of interest related to this article.

REFERENCES


